

Stylish Concurrency
using
Functional programming

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Agenda

- Concurrency and parallelism
- A simple scraper
- Effects
- Optimizing the scraper
- Massive Parallelism
- Evaluation
- Monoids
- Functors
- Applicative Functors
- Monads
- FP Intuition
- Conclusion

References

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<http://haskellbook.com/>

<https://underscore.io/books/scala-with-cats/>

<https://typelevel.org/cats/>

Concurrency and Parallelism

Task 1



Task 2



Task 3



Concurrency and Parallelism

Task 1



Task 2



Task 3



Concurrency and Parallelism

Task 1



Task 2



Task 3



Concurrency and Parallelism

Task 1



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Task 3



Concurrency and Parallelism

Task 1



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Task 3



Concurrency and Parallelism

Task 1



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Task 3



Concurrency and Parallelism

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Concurrency and Parallelism

Task 1



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Concurrency and Parallelism

Task 1



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Concurrency and Parallelism

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Concurrency and Parallelism

Task 1



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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

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Concurrency and Parallelism

Task 1



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Concurrency and Parallelism

Task 1



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Task 3



Concurrency and Parallelism

Task 1



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Task 3



Concurrency and Parallelism

Task 1



Task 2



Task 3



Concurrency and Parallelism

Task 1



Task 2



Task 3



"Simplicity is
prerequisite for reliability."

-Edsger W. Dijkstra

A simple scraper

A simple scraper

Authentication

A simple scraper

Authentication



First Page

A simple scraper

Authentication



First Page



Second Page

A simple scraper

Authentication



First Page



Second Page



Result

A simple scraper

A simple scraper

Authentication



First Page



Second Page



Result

A simple scraper

Authentication



First Page



Second Page



Result

```
def authenticate(username: String, password: String): AsyncEffect[Token] = ...
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent] = ...
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result] = ...
```


A simple scraper

Authentication



First Page



Second Page



Result

```
def authenticate(username: String, password: String): AsyncEffect[Token] = ...
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent] = ...
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result] = ...
```

```
authenticate("tdc", "2019").flatMap { token =>  
  scrapePage("page1", token).flatMap { firstPage =>  
    scrapePage("page2", token).flatMap { secondPage =>  
      mergePages(List(firstPage, secondPage))  
    }  
  }  
}
```


A simple scraper

Authentication



First Page



Second Page



Result

```
def authenticate(username: String, password: String): AsyncEffect[Token] = ...
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent] = ...
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result] = ...
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token)
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Effects

Effects

1

Effects

1

1 2 3

Effects

1

1.5

1 2 3

Effects

1

1.5

'A'

1 2 3

Effects

1

1.5

Any

'A'

1 2 3

Effects

1

1.5

Any

'A'

1 'b'

1 2 3

Effects

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>  
  scrapePage("page1", token).flatMap { firstPage =>  
    scrapePage("page2", token ).flatMap { secondPage =>  
      mergePages(List(firstPage, secondPage))  
    }  
  }  
}
```

```
for {  
  token <- authenticate("tdc", "2019")  
  firstPage <- scrapePage("page1", token)  
  secondPage <- scrapePage("page2", token )  
  result <- mergePages(List(firstPage, secondPage))  
} yield result
```


ES6 Promise

```
def authenticate(username: String, password: String): Promise[Token]
```

```
def scrapePage(url: String, token: Token): Promise[PageContent]
```

```
def mergePages(pages: List[PageContent]): Promise[Result]
```

```
authenticate("tdc", "2019").then { token =>  
  scrapePage("page1", token).then { firstPage =>  
    scrapePage("page2", token ).then { secondPage =>  
      mergePages(List(firstPage, secondPage))  
    }  
  }  
}
```

```
for {  
  token <- authenticate("tdc", "2019")  
  firstPage <- scrapePage("page1", token)  
  secondPage <- scrapePage("page2", token )  
  result <- mergePages(List(firstPage, secondPage))  
} yield result
```


Scala Promise (a.k.a Future)

```
def authenticate(username: String, password: String): Future[Token]
```

```
def scrapePage(url: String, token: Token): Future[PageContent]
```

```
def mergePages(pages: List[PageContent]): Future[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token ).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token )
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Rx Scala

```
def authenticate(username: String, password: String): Observable[Token]
```

```
def scrapePage(url: String, token: Token): Observable[PageContent]
```

```
def mergePages(pages: List[PageContent]): Observable[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token)
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Java/Kotlin Reactor Mono

```
def authenticate(username: String, password: String): Mono<Token>
```

```
def scrapePage(url: String, token: Token): Mono<PageContent>
```

```
def mergePages(pages: List[PageContent]): Mono<Result>
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token ).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token )
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Scala cats-effect IO (Fibers)

```
def authenticate(username: String, password: String): IO[Token]
```

```
def scrapePage(url: String, token: Token): IO[PageContent]
```

```
def mergePages(pages: List[PageContent]): IO[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token)
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Scala ZIO (Fibers)

```
def authenticate(username: String, password: String): ZIO[R, E, Token]
```

```
def scrapePage(url: String, token: Token): ZIO[R, E, PageContent]
```

```
def mergePages(pages: List[PageContent]): ZIO[R, E, Result]
```

```
authenticate("tdc", "2019").flatMap { token =>
  scrapePage("page1", token).flatMap { firstPage =>
    scrapePage("page2", token ).flatMap { secondPage =>
      mergePages(List(firstPage, secondPage))
    }
  }
}
```

```
for {
  token <- authenticate("tdc", "2019")
  firstPage <- scrapePage("page1", token)
  secondPage <- scrapePage("page2", token )
  result <- mergePages(List(firstPage, secondPage))
} yield result
```


Haskell IO

Haskell MVar

Haskell STM

Scala ZIO STM

Scala ZIO Ref

Scala ZIO Stream

Scala Twitter Future

Scala Monix

Optimizing the scraper

Optimizing the scraper

Authentication



First Page



Second Page

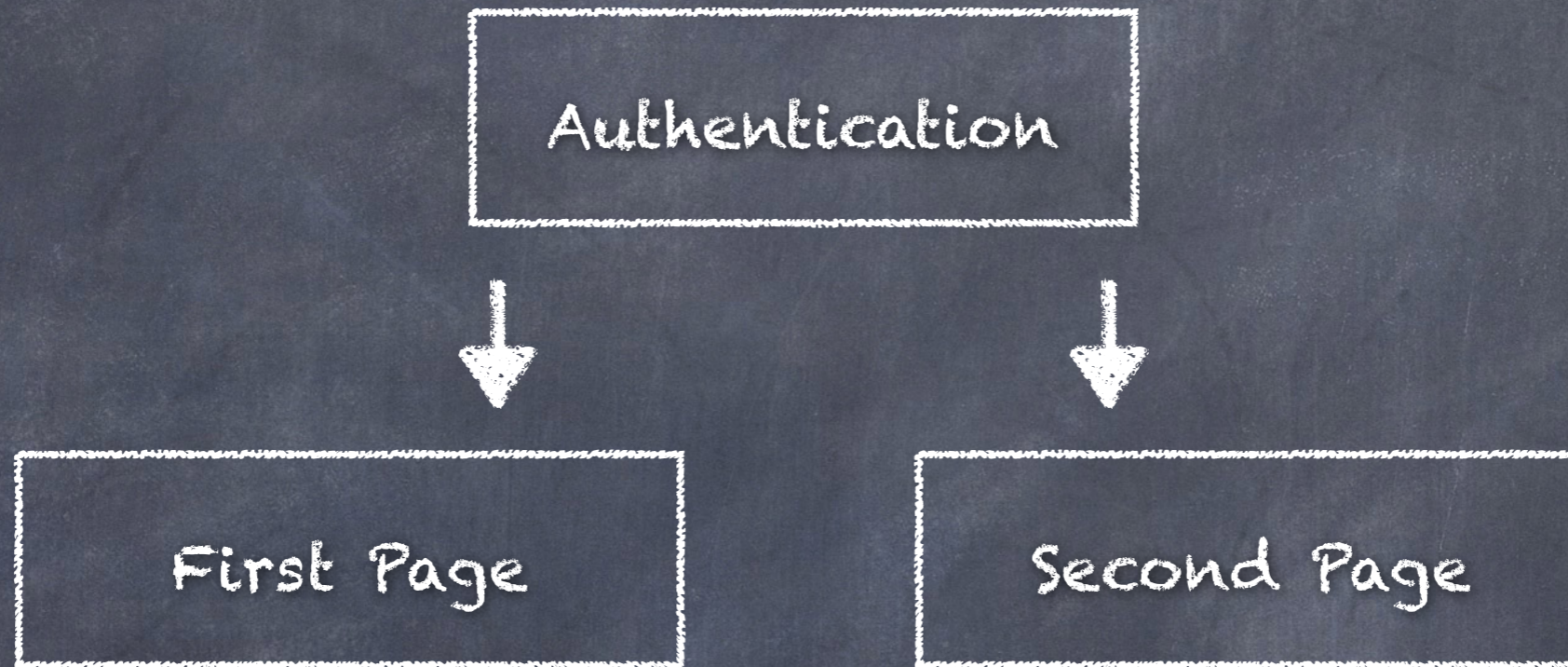


Result

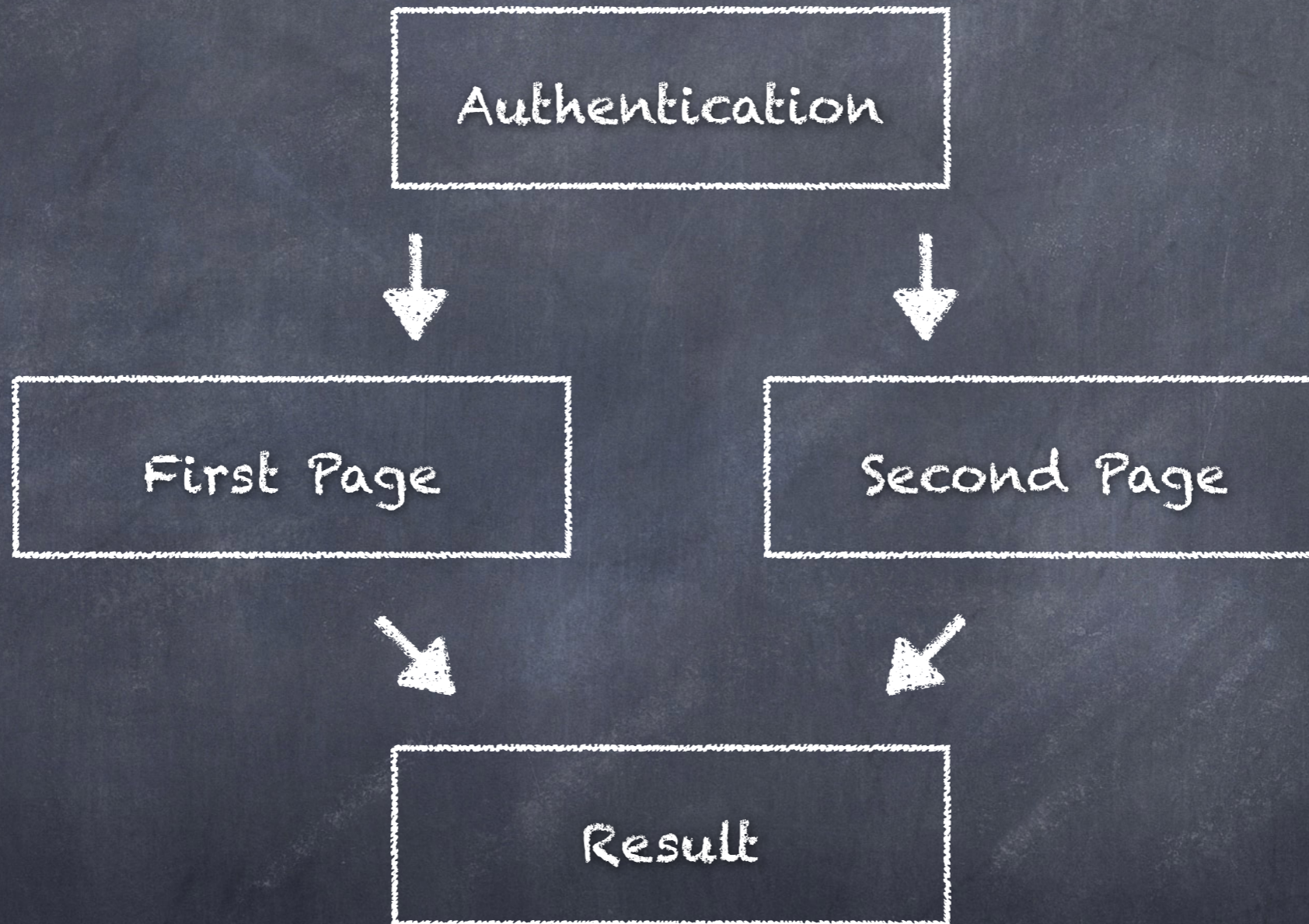
Optimizing the scraper

Authentication

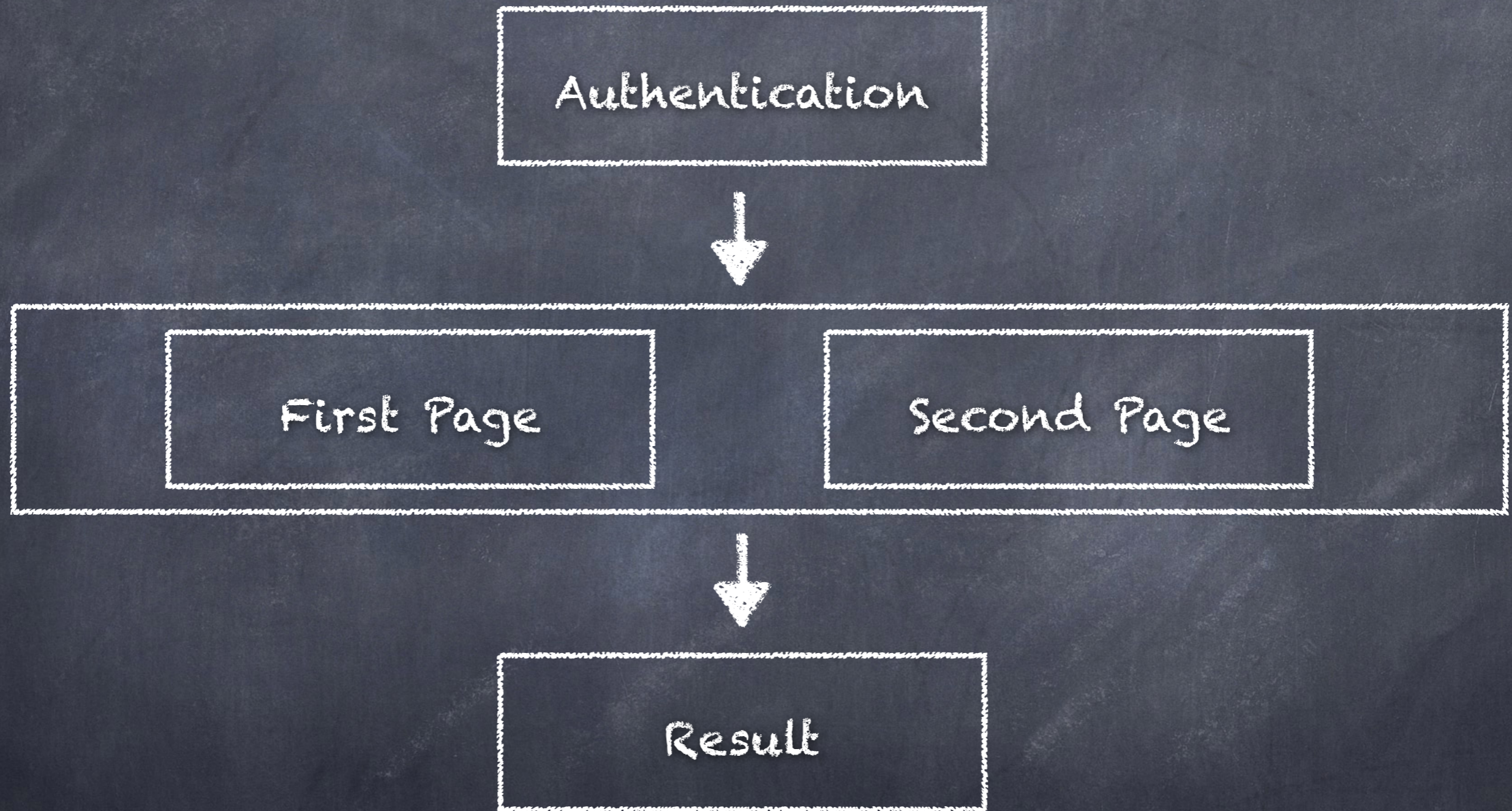
Optimizing the scraper



Optimizing the scraper



Optimized scraper



Parallelizing the scraper

Parallelizing the scraper

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```


Parallelizing the scraper

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>  
  (scrapePage("page1", token) zip scrapePage("page2", token))  
  .flatMap { tuple =>  
    mergePages(tuple.productIterator.toList)  
  }  
}
```


Parallelizing the scraper

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(url: String, token: Token): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
authenticate("tdc", "2019").flatMap { token =>  
  (scrapePage("page1", token) zip scrapePage("page2", token))  
  .flatMap { tuple =>  
    mergePages(tuple.productIterator.toList)  
  }  
}
```

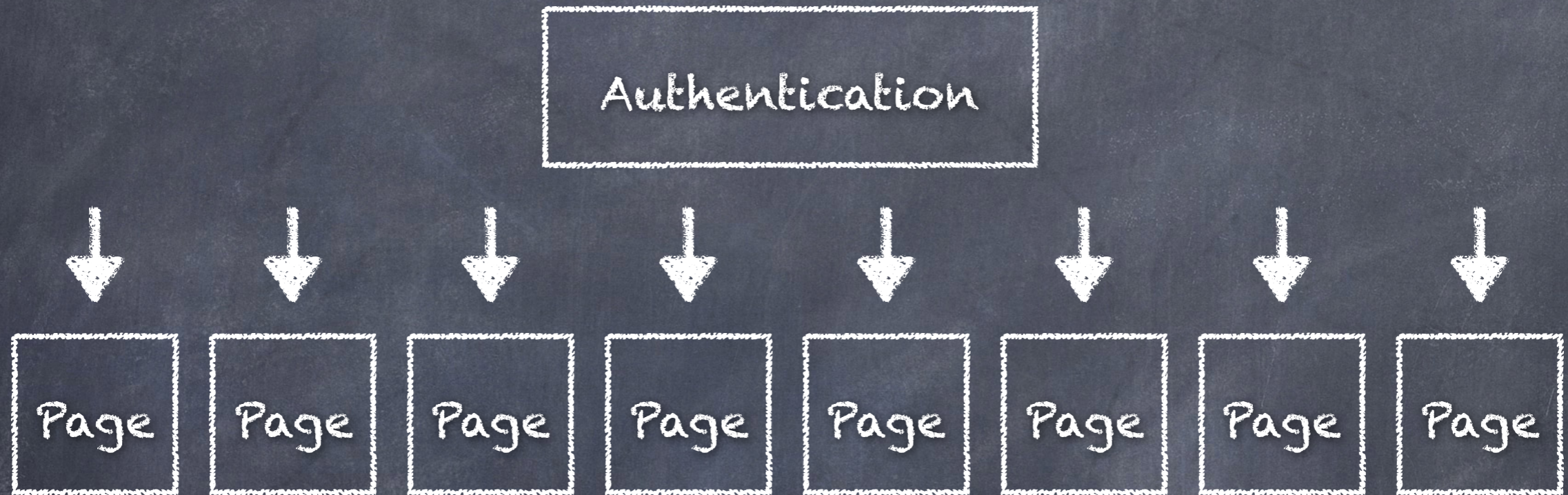
```
for {  
  token <- authenticate("tdc", "2019")  
  tuple <- scrapePage("page1", token) zip scrapePage("page2", token )  
  result <- mergePages(tuple.productIterator.toList)  
} yield result
```


Massive Parallelism

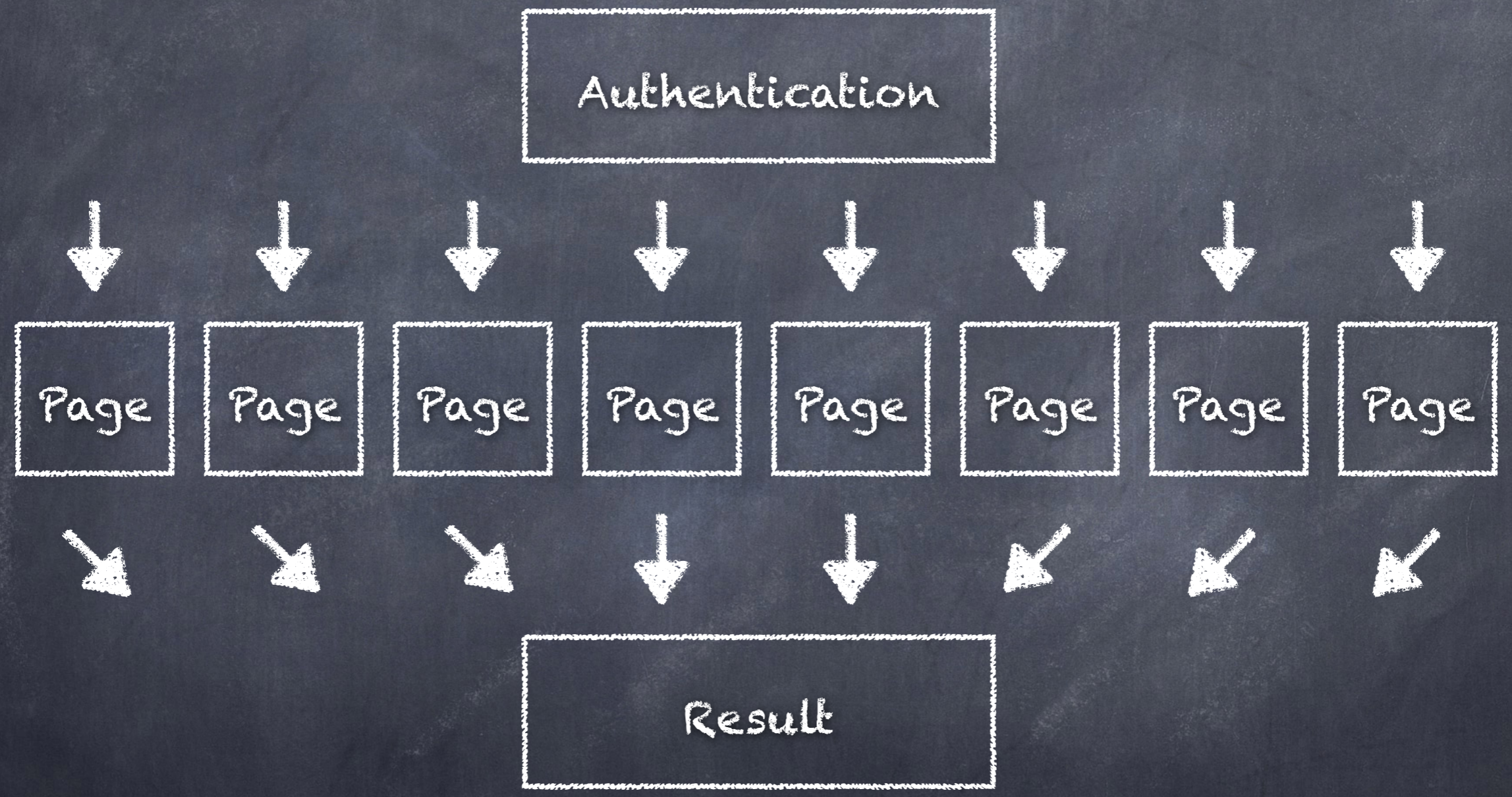
Massive Parallelism

Authentication

Massive Parallelism



Massive Parallelism



Massive Parallelism Opportunity

Authentication



Page

Page

Page

Page

Page

Page

Page

Page



Result

High Throughput through Parallelism

High Throughput through Parallelism

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(token: Token)(url: String): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```


High Throughput through Parallelism

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(token: Token)(url: String): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
val urls: List[String] = ... // 1000 Urls
```


High Throughput through Parallelism

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(token: Token)(url: String): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
val urls: List[String] = ... // 1000 Urls
```

```
authenticate("tdc", "2019").flatMap { token =>  
  AsyncEffect  
    .traverse(urls)(scrapePage(token))  
    .flatMap { list : List[PageContent] =>  
      mergePages(list)  
    }  
}
```


High Throughput through Parallelism

```
def authenticate(username: String, password: String): AsyncEffect[Token]
```

```
def scrapePage(token: Token)(url: String): AsyncEffect[PageContent]
```

```
def mergePages(pages: List[PageContent]): AsyncEffect[Result]
```

```
val urls: List[String] = ... // 1000 Urls
```

```
authenticate("tdc", "2019").flatMap { token =>  
  AsyncEffect  
    .traverse(urls)(scrapePage(token))  
    .flatMap { list : List[PageContent] =>  
      mergePages(list)  
    }  
}
```

```
for {  
  token <- authenticate("tdc", "2019")  
  list <- AsyncEffect.traverse(urls)(scrapePage(token))  
  result <- mergePages(list)  
} yield result
```


Expression Evaluation

Expression Evaluation

```
def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)
```


Evaluation

```
def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)
```

```
expr(10, 20, 30)
```


Imperative Evaluation

```
def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)
```

```
expr(10, 20, 30)
```


Imperative Evaluation

```
def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)
```

`expr(10, 20, 30)`



`(10 + 30) + (b + c) + (a + b)`

Imperative Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



(10 + 30) + (b + c) + (a + b)



40 + (20 + 30) + (a + b)

Imperative Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



(10 + 30) + (b + c) + (a + b)



40 + (20 + 30) + (a + b)



40 + 50 + (a + b)

Imperative Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



(10 + 30) + (b + c) + (a + b)



40 + (20 + 30) + (a + b)



40 + 50 + (a + b)



40 + 50 + (10 + 20)

Imperative Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



(10 + 30) + (b + c) + (a + b)



40 + (20 + 30) + (a + b)



40 + 50 + (a + b)



40 + 50 + (10 + 20)



40 + 50 + 30

Imperative Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



(10 + 30) + (b + c) + (a + b)



40 + (20 + 30) + (a + b)



40 + 50 + (a + b)



40 + 50 + (10 + 20)



40 + 50 + 30



120

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



$\lambda.abc = (a + c) + (b + c) + (a + b)$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



$\lambda.abc = (a + c) + (b + c) + (a + b)$



$\lambda.10bc = (10 + c) + (b + c) + (10 + b)$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



$\lambda.abc = (a + c) + (b + c) + (a + b)$



$\lambda.10bc = (10 + c) + (b + c) + (10 + b)$



$\lambda.1020c = (10 + c) + (20 + c) + (10 + 20)$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



$\lambda.abc = (a + c) + (b + c) + (a + b)$



$\lambda.10bc = (10 + c) + (b + c) + (10 + b)$



$\lambda.1020c = (10 + c) + (20 + c) + (10 + 20)$



$\lambda.1020c = (10 + c) + (20 + c) + 30$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)

expr(10, 20, 30)



$\lambda.abc = (a + c) + (b + c) + (a + b)$



$\lambda.10bc = (10 + c) + (b + c) + (10 + b)$



$\lambda.1020c = (10 + c) + (20 + c) + (10 + 20)$



$\lambda.1020c = (10 + c) + (20 + c) + 30$



$\lambda.102030 = (10 + 30) + (20 + 30) + 30$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)



$$\lambda.102030 = (10 + 30) + (20 + 30) + 30$$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)



$$\lambda.102030 = (10 + 30) + (20 + 30) + 30$$



$$\lambda.102030 = 50 + 40 + 30$$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)



$$\lambda.102030 = (10 + 30) + (20 + 30) + 30$$



$$\lambda.102030 = 50 + 40 + 30$$



$$\lambda.102030 = 120$$

λ -Calculus Evaluation

def expr(a: Int, b: Int, c: Int): Int = (a + c) + (b + c) + (a + b)



$$\lambda.102030 = (10 + 30) + (20 + 30) + 30$$



$$\lambda.102030 = 50 + 40 + 30$$



$$\lambda.102030 = 120$$

Imperative

Imperative

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



120

Imperative

λ -Calculus

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



120

Imperative

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



120

λ -Calculus

$\text{expr}(10, 20, 30)$

Imperative

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



120

λ -Calculus

$\text{expr}(10, 20, 30)$



$\lambda.abc = (a + c) + (b + c) + (a + b)$

Imperative

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



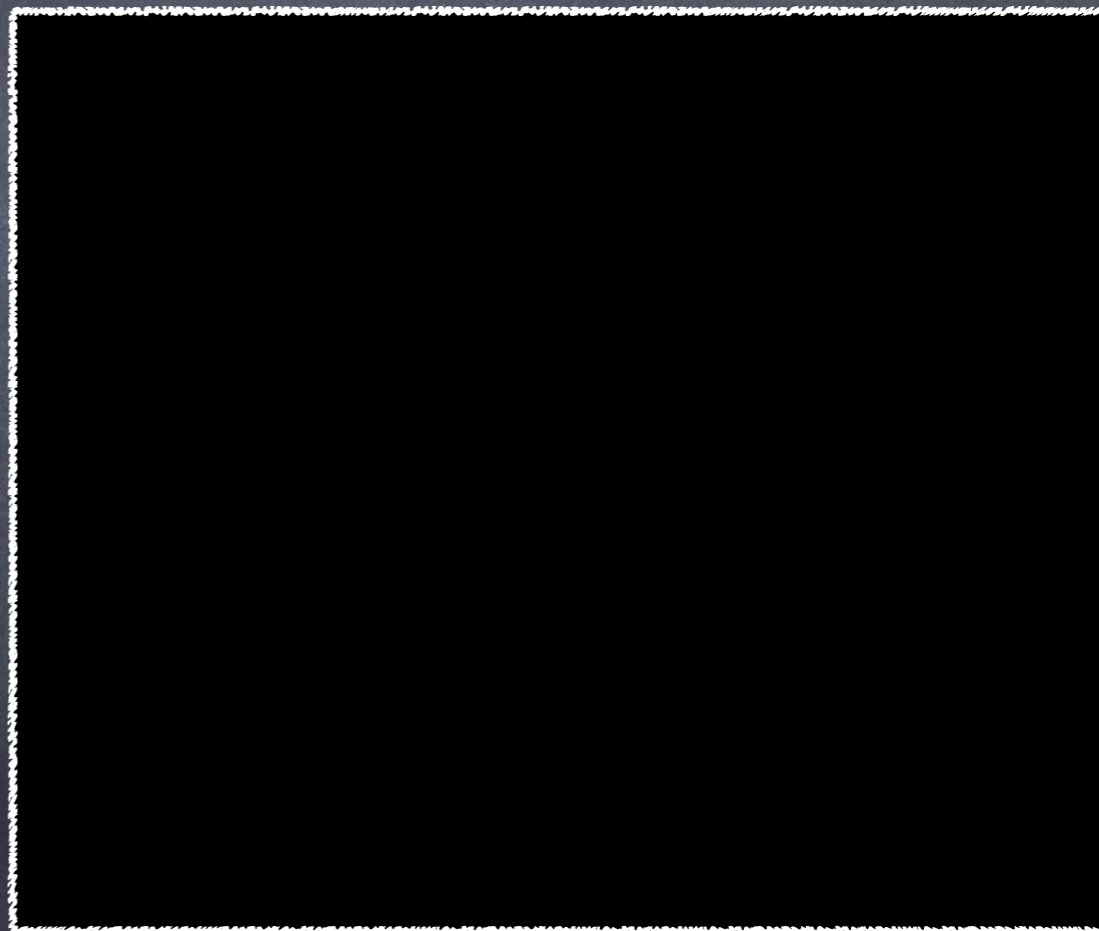
120

λ -Calculus

$\text{expr}(10, 20, 30)$



$\lambda.abc = (a + c) + (b + c) + (a + b)$



Imperative

$\text{expr}(10, 20, 30)$



$(10 + 30) + (b + c) + (a + b)$



$40 + (20 + 30) + (a + b)$



$40 + 50 + (a + b)$



$40 + 50 + (10 + 20)$



$40 + 50 + 30$



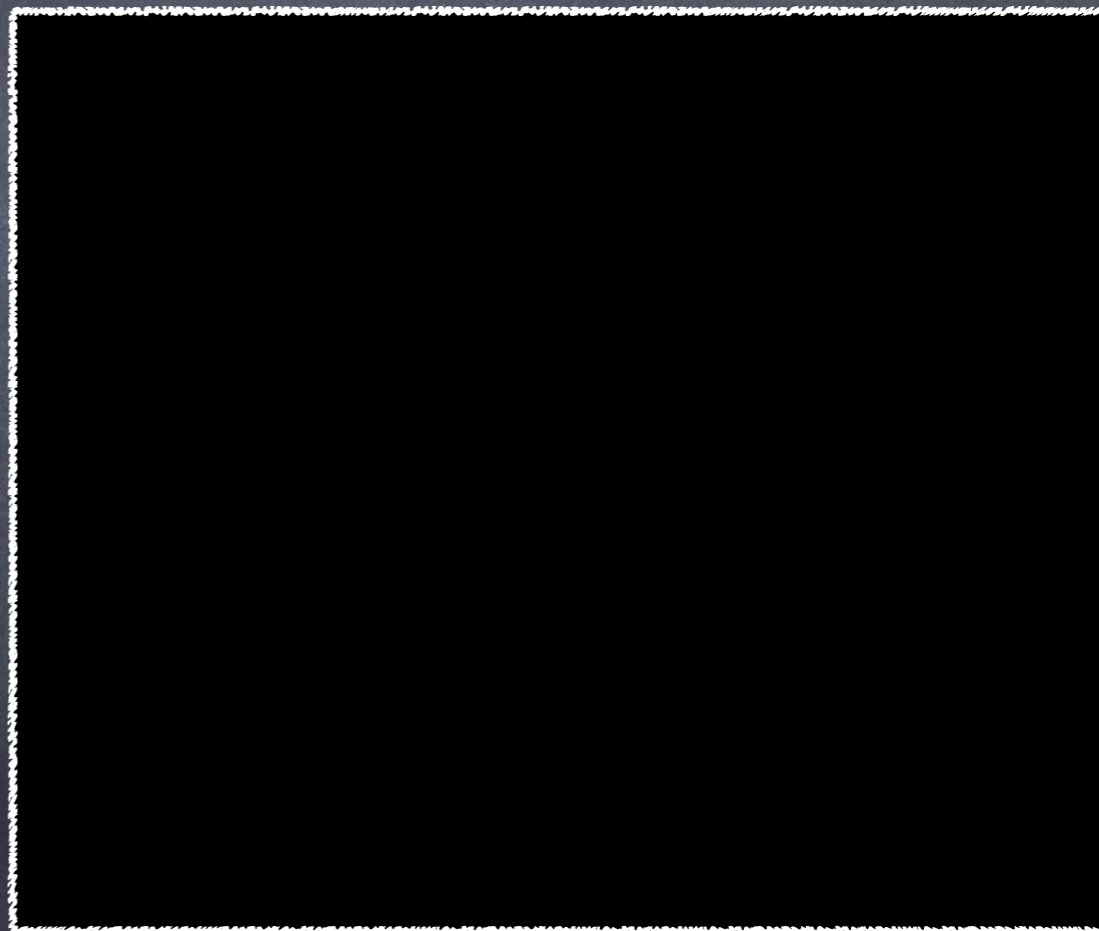
120

λ -Calculus

$\text{expr}(10, 20, 30)$



$\lambda.abc = (a + c) + (b + c) + (a + b)$



120

In functional programming,
EVERYTHING is an **EXPRESSION**.

Monoids

Monoids

```
trait Monoid[A] {  
  def mappend(x: A, y: A): A  
  def mempty: A  
}
```


Monoids

```
trait Monoid[A] {  
  def mappend(x: A, y: A): A  
  def mempty: A  
}
```

$$1 + (2 + 3) = (1 + 2) + 3$$

$$1 + 0 = 1 + 0$$

Monoids

```
trait Monoid[A] {  
  def mappend(x: A, y: A): A  
  def mempty: A  
}
```

$$1 + (2 + 3) = (1 + 2) + 3$$

$$1 + 0 = 1 + 0$$

$$3 * (2 * 3) = (3 * 2) * 3$$

$$3 * 1 = 3 * 1$$

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```


Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Expr <> R <> Expr <> R <> Expr

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Expr <> R <> Expr <> R <> Expr

R <> R <> Expr <> R <> R

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Expr <> R <> Expr <> R <> Expr

R <> R <> Expr <> R <> R

RR <> R <> RR

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Expr <> R <> Expr <> R <> Expr

R <> R <> Expr <> R <> R

RR <> R <> RR

RRR <> RR

Monoids

```
trait Monoid[Expr] {  
  def <>(x: Expr, y: Expr): Expr  
  def mempty: Expr  
}
```

Expr <> Expr <> Expr <> Expr <> Expr

Expr <> R <> Expr <> R <> Expr

R <> R <> Expr <> R <> R

RR <> R <> RR

RRR <> RR

RRRRR

Monoids

Monoids

$\text{Expr} \langle \rangle \text{Expr} \langle \rangle \text{Error} \langle \rangle \text{Expr} \langle \rangle \text{Expr} = \text{Error}$

Monoids

$\text{Expr} \langle \rangle \text{Expr} \langle \rangle \text{Error} \langle \rangle \text{Expr} \langle \rangle \text{Expr} = \text{Error}$

$\text{Error} \langle \rangle \text{R} \langle \rangle \text{Expr} \langle \rangle \text{R} \langle \rangle \text{Expr} = \text{Error}$

Monoids

$\text{Expr} \langle \rangle \text{Expr} \langle \rangle \text{Error} \langle \rangle \text{Expr} \langle \rangle \text{Expr} = \text{Error}$

$\text{Error} \langle \rangle \text{R} \langle \rangle \text{Expr} \langle \rangle \text{R} \langle \rangle \text{Expr} = \text{Error}$

$\text{R} \langle \rangle \text{R} \langle \rangle \text{R} \langle \rangle \text{Error} \langle \rangle \text{R} = \text{Error}$

Functors

Functors

```
trait Functor[F[_]] {  
  def map[A, B](fa: F[A])(f: A => B): F[B]  
}
```


Functors

```
trait Functor[F[_]] {  
  def map[A, B](fa: F[A])(f: A => B): F[B]  
}
```

```
def toB(a: A): B = ...
```


Functors

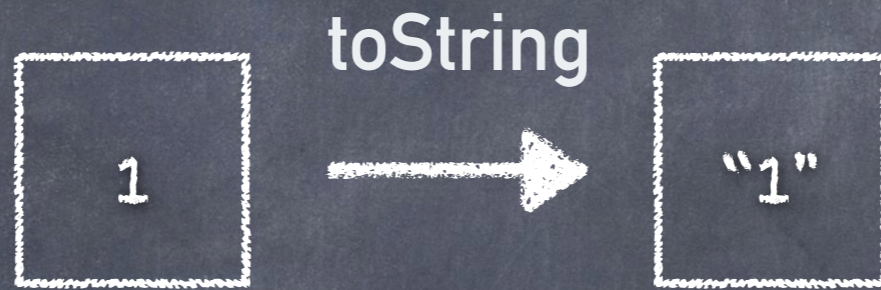
```
trait Functor[F[_]] {  
  def map[A, B](fa: F[A])(f: A => B): F[B]  
}
```

```
  def toB(a: A): B = ...
```

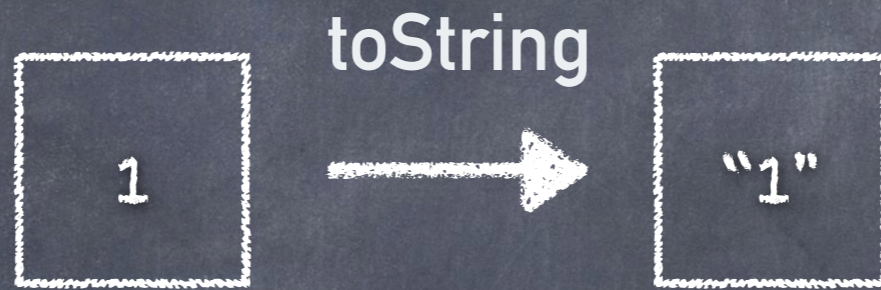
```
  val fb: F[B] = F[A].map(toB)
```


Functors

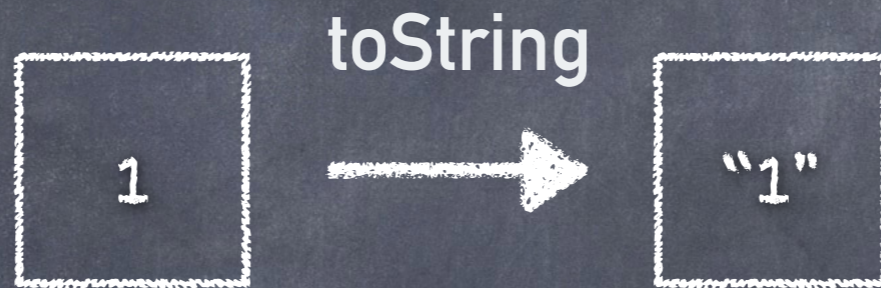
Functors



Functors



Functors



Functors

Functors

1

Functors



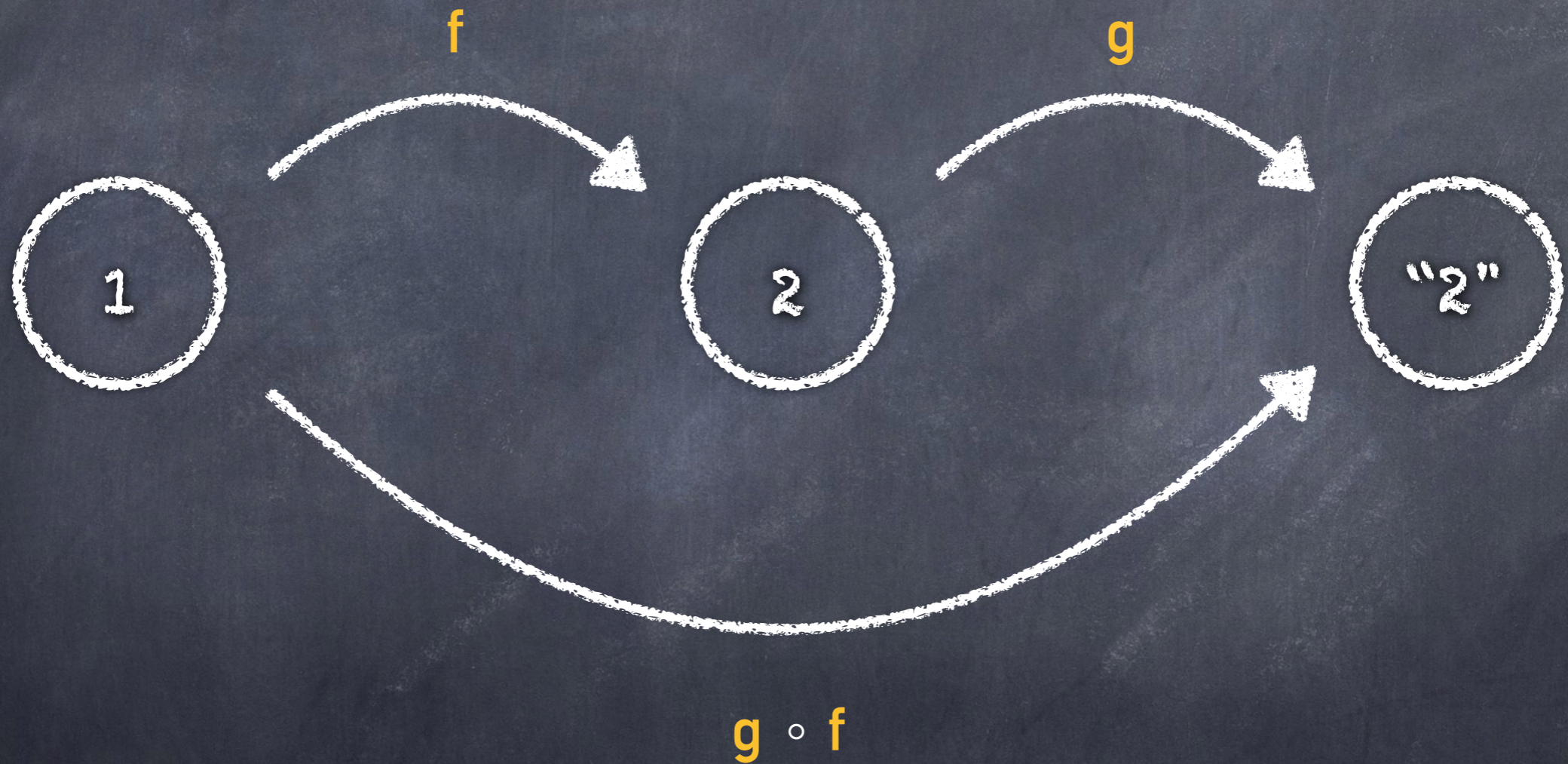
Functors



Functors



Functors



Applicative Functors

Applicative Functors

```
trait Applicative[F[_]] extends Functor[F] {  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)]  
  def pure[A](a: A): F[A]  
}
```


Applicative Functors

```
trait Applicative[F[_]] extends Functor[F] {  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)]  
  def pure[A](a: A): F[A]  
}
```

```
val liftedInt: F[Int] = F.pure(1)
```


Applicative Functors

```
trait Applicative[F[_]] extends Functor[F] {  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)]  
  def pure[A](a: A): F[A]  
}
```

```
val liftedInt: F[Int] = F.pure(1)
```

```
val liftedString: F[String] = F.pure("a")
```


Applicative Functors

```
trait Applicative[F[_]] extends Functor[F] {  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)]  
  def pure[A](a: A): F[A]  
}
```

```
val liftedInt: F[Int] = F.pure(1)
```

```
val liftedString: F[String] = F.pure("a")
```

```
val res: F[(Int,String)] = F.product(liftedInt, liftedString)
```


Applicative Functors

Applicative Functors



Applicative Functors

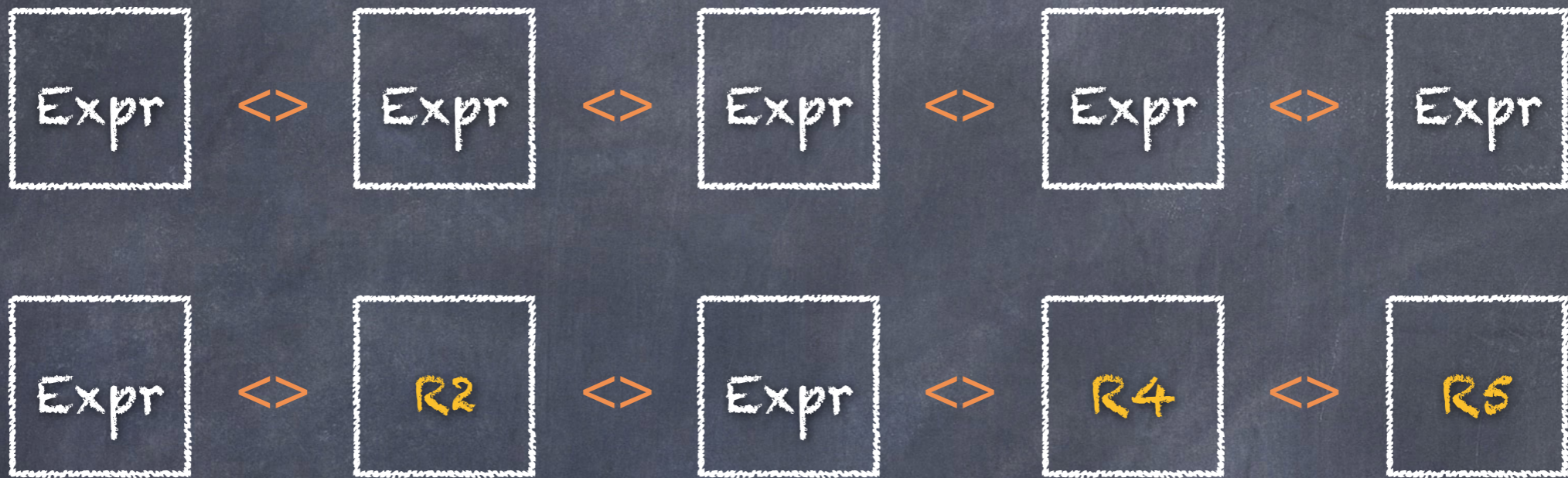


Applicative Functors

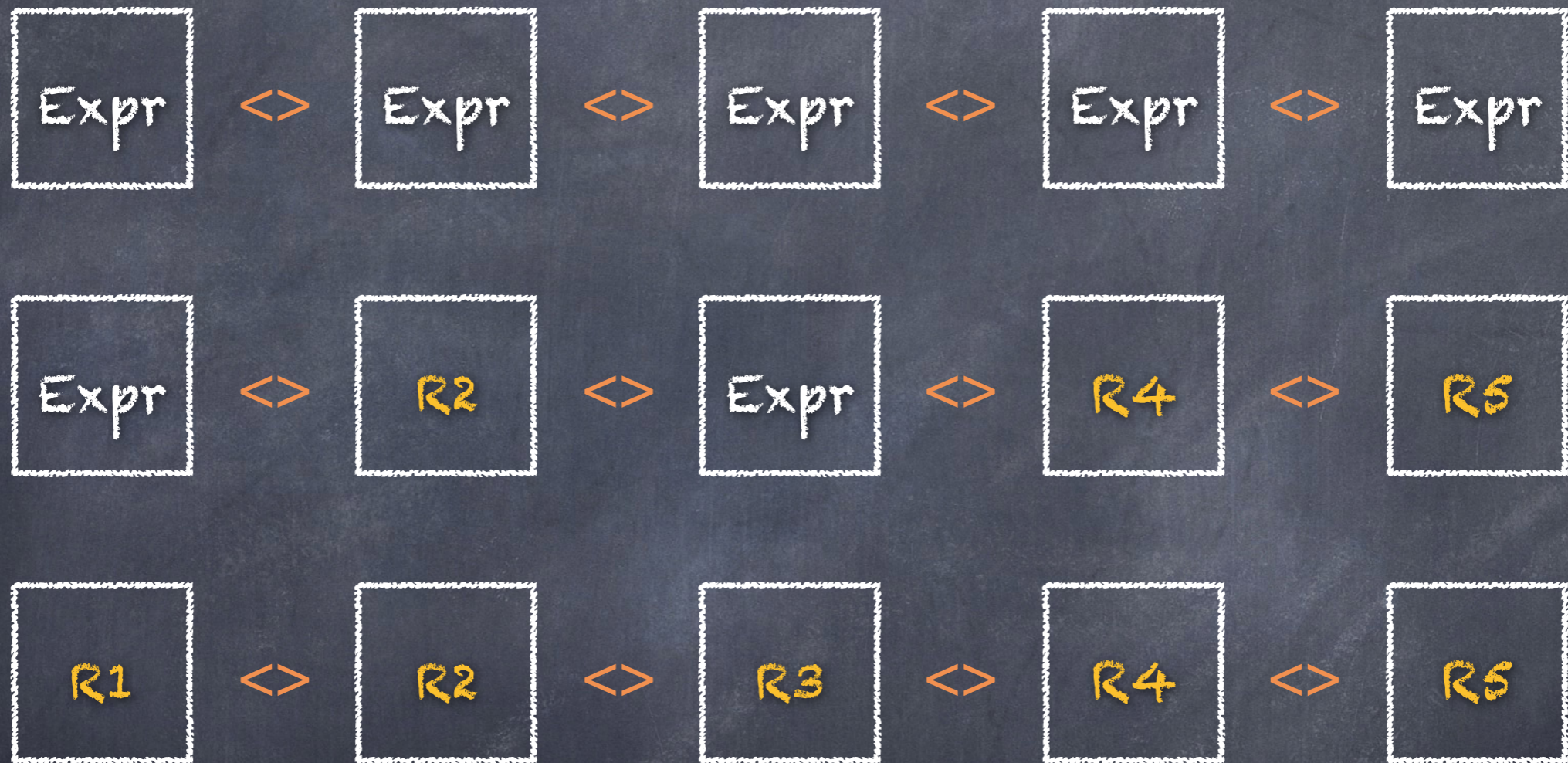
Applicative Functors



Applicative Functors



Applicative Functors



Applicative Functors



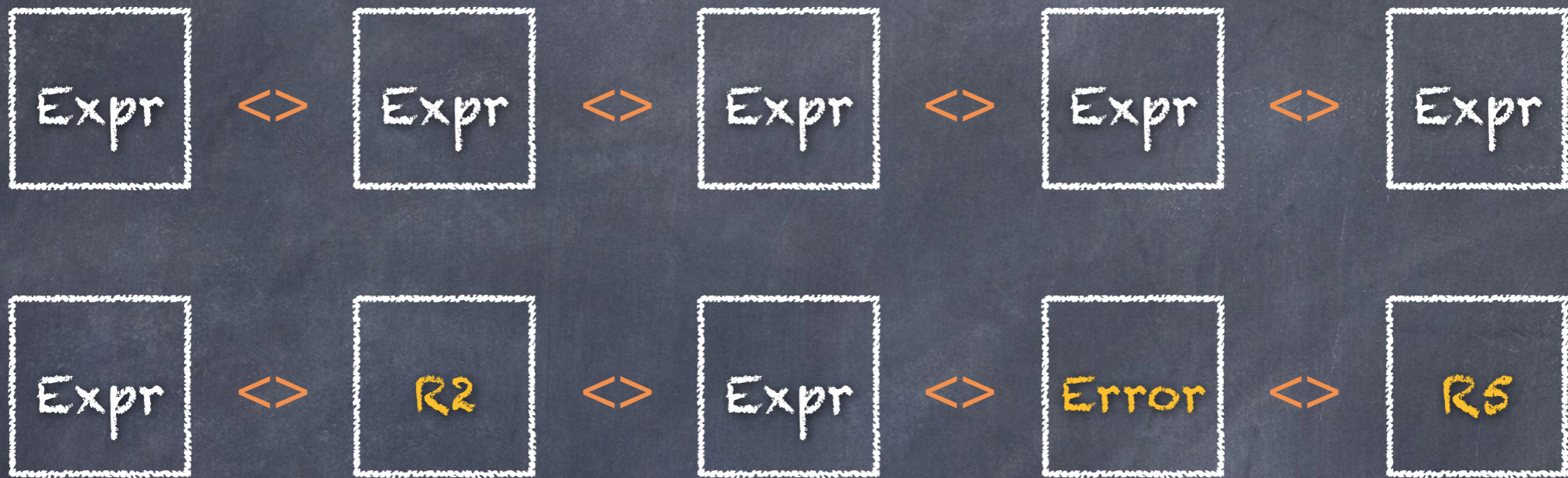
$(R1, R2, R3, R4, R5)$

Applicative Functors

Applicative Functors



Applicative Functors



Applicative Functors



Applicative Functors

Applicative Functors

Authenticate

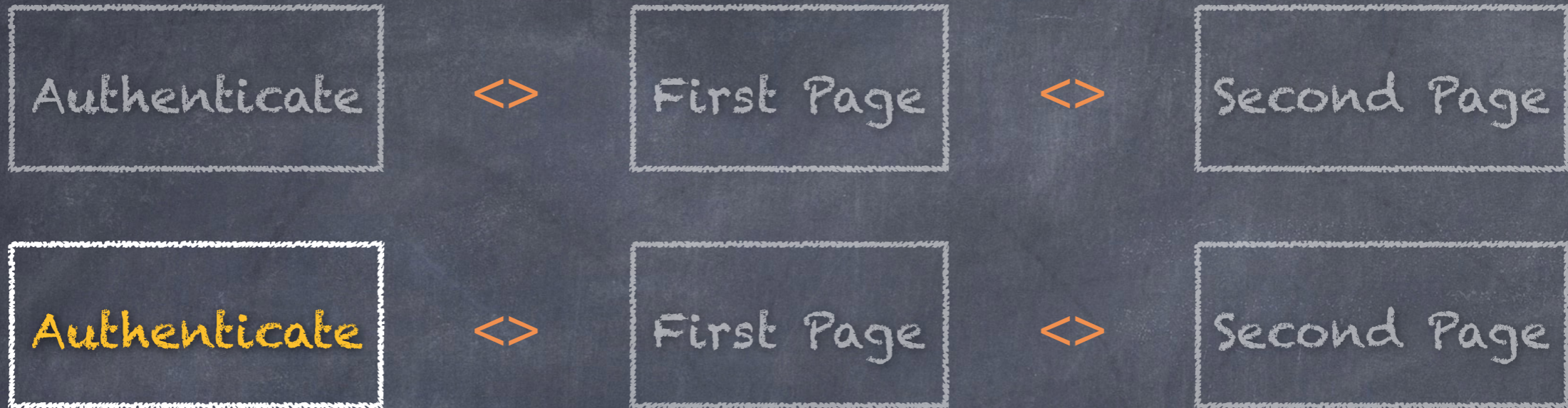
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First Page

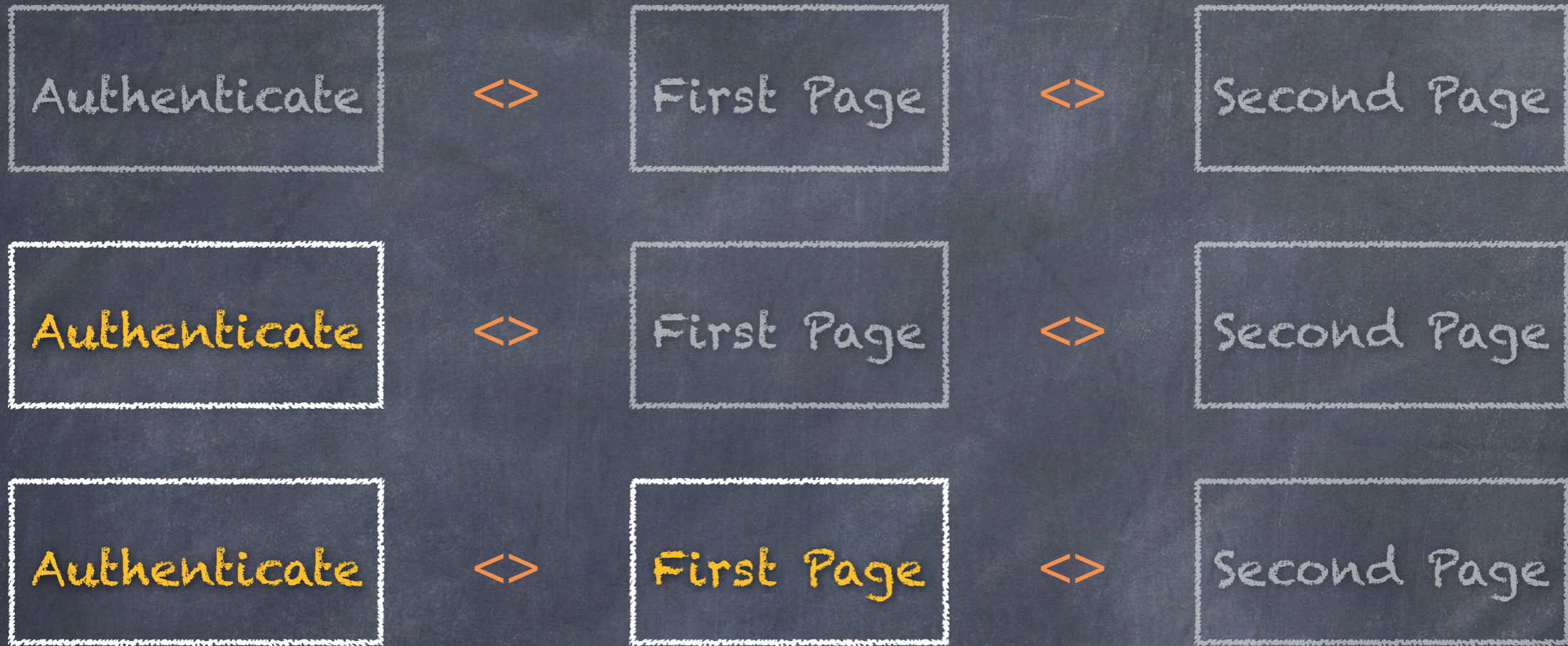
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Second Page

Applicative Functors



Applicative Functors



Applicative Functors



Applicative Functors

Authenticate <> First Page <> Second Page

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(token, page1, page) \xrightarrow{f} Result

Applicative Functors

Applicative Functors

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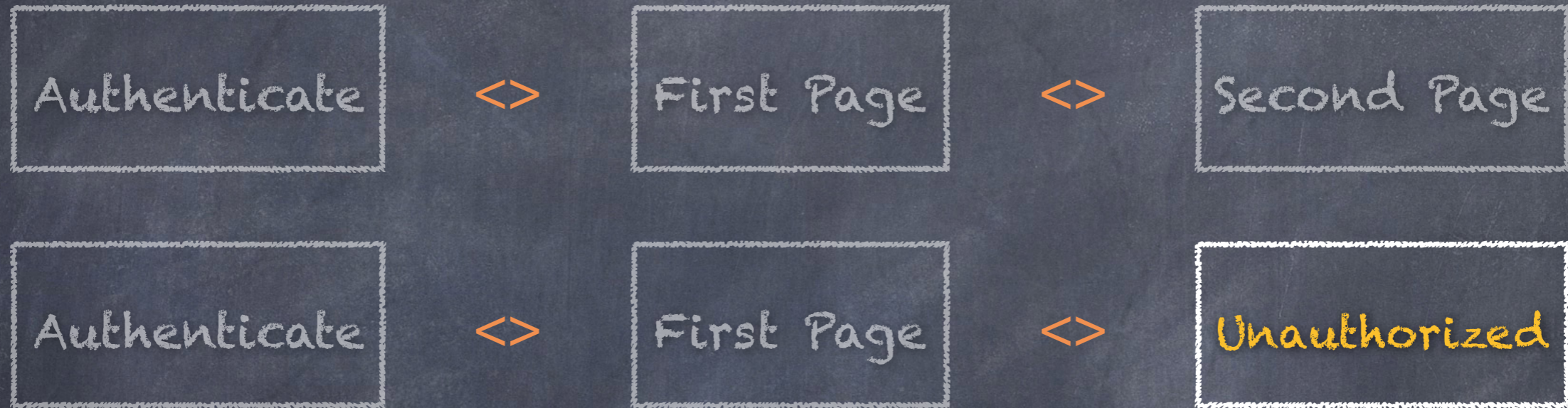


First Page

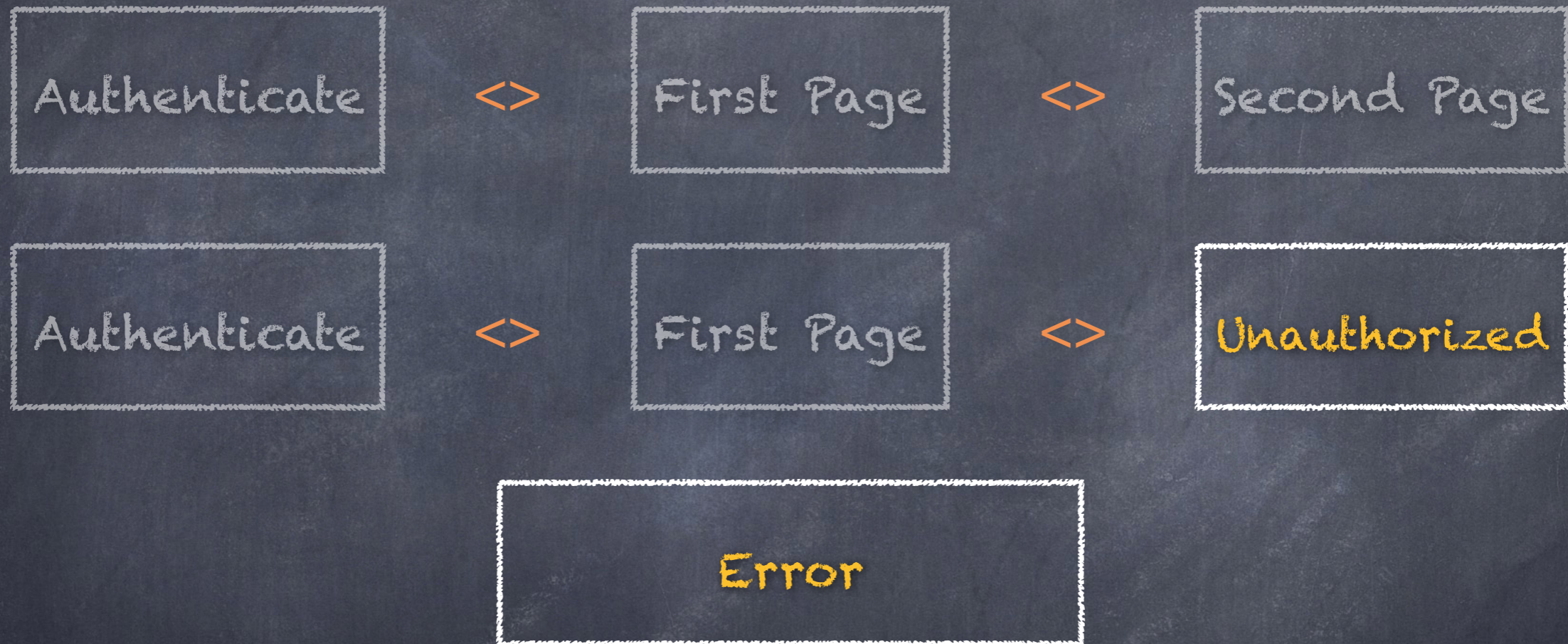


Second Page

Applicative Functors



Applicative Functors



Monads

Monads

```
trait Monad[F[_]] {  
  def flatMap[A, B](a: A): F[B]  
  def return[A](a: A): F[A]  
}
```


Monads

```
trait Monad[F[_]] {  
  def flatMap[A, B](a: A): F[B]  
  def return[A](a: A): F[A]  
}
```

```
val liftedInt: F[Int] = F.return(1)
```


Monads

```
trait Monad[F[_]] {  
  def flatMap[A, B](a: A): F[B]  
  def return[A](a: A): F[A]  
}
```

```
val liftedInt: F[Int] = F.return(1)
```

```
val liftedString: F[String] = liftedInt.flatMap(a => F.return(a.toString))
```


Monads

Monads



Monads



Monads

return and pure are the same
function!

Monads

Monads



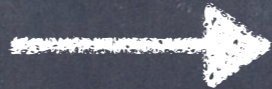
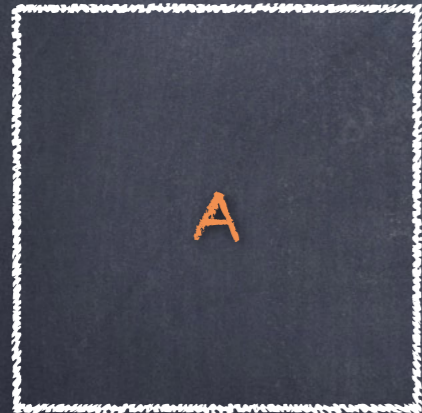
Monads

Expr

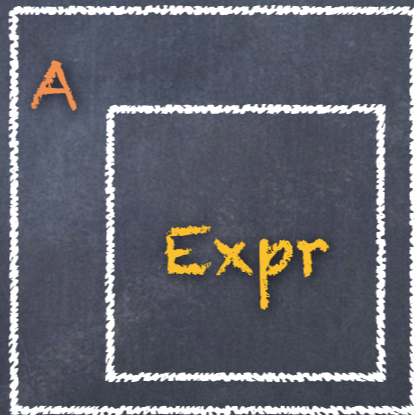
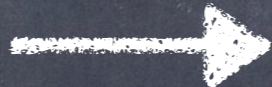


A

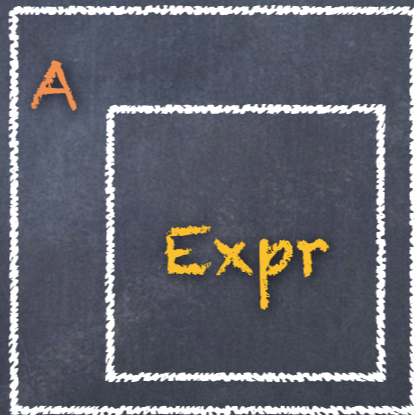
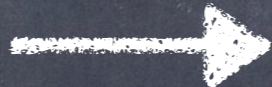
Monads



Monads



Monads



Monads

Monads



Monads

Expr



Error

Monads

Expr



Error



Error

Monads

Monads

Authenticate



First Page



Second Page

Monads

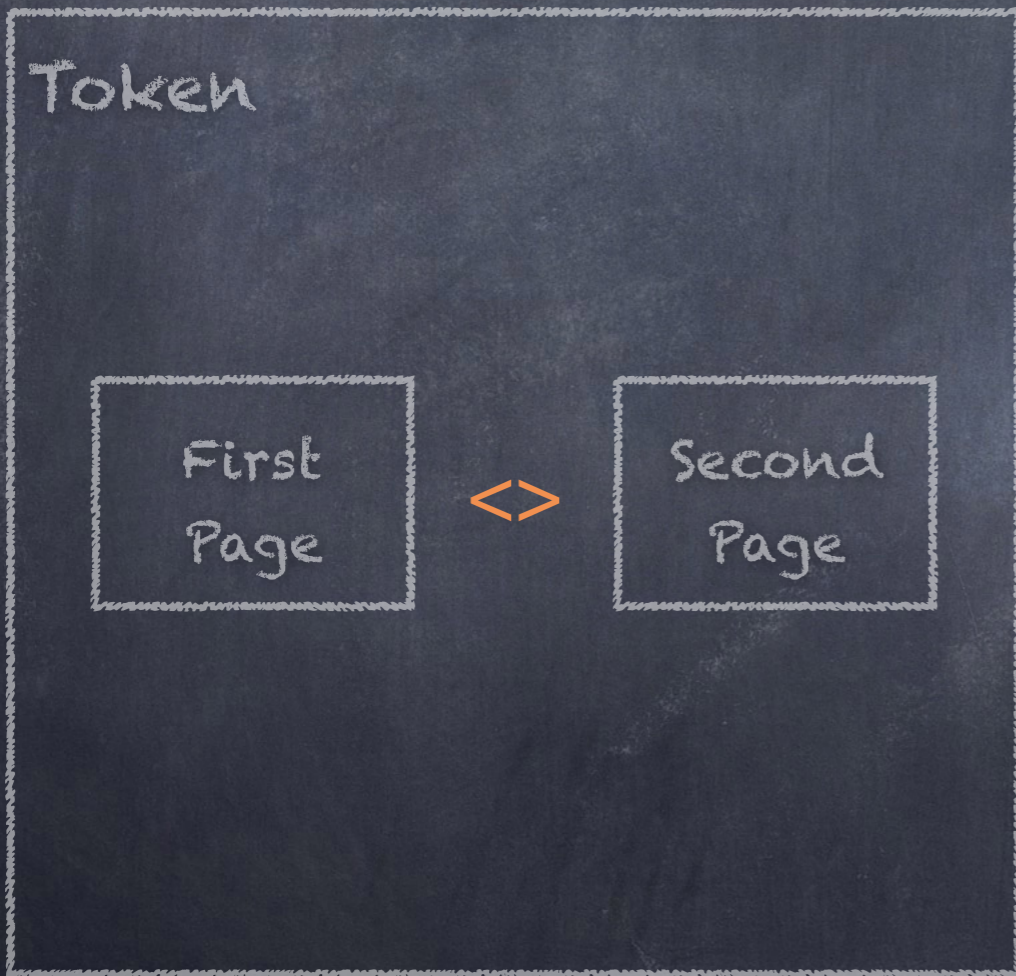
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First Page



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Monads

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Monads

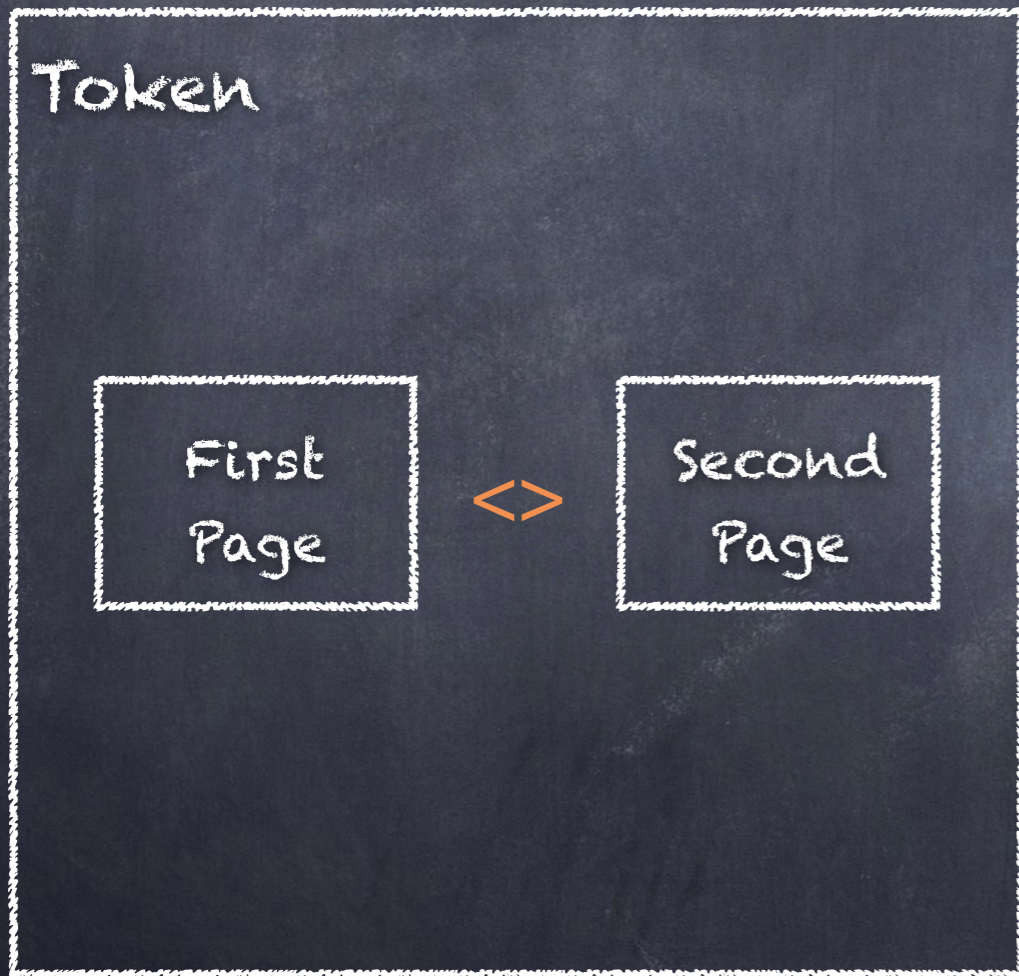
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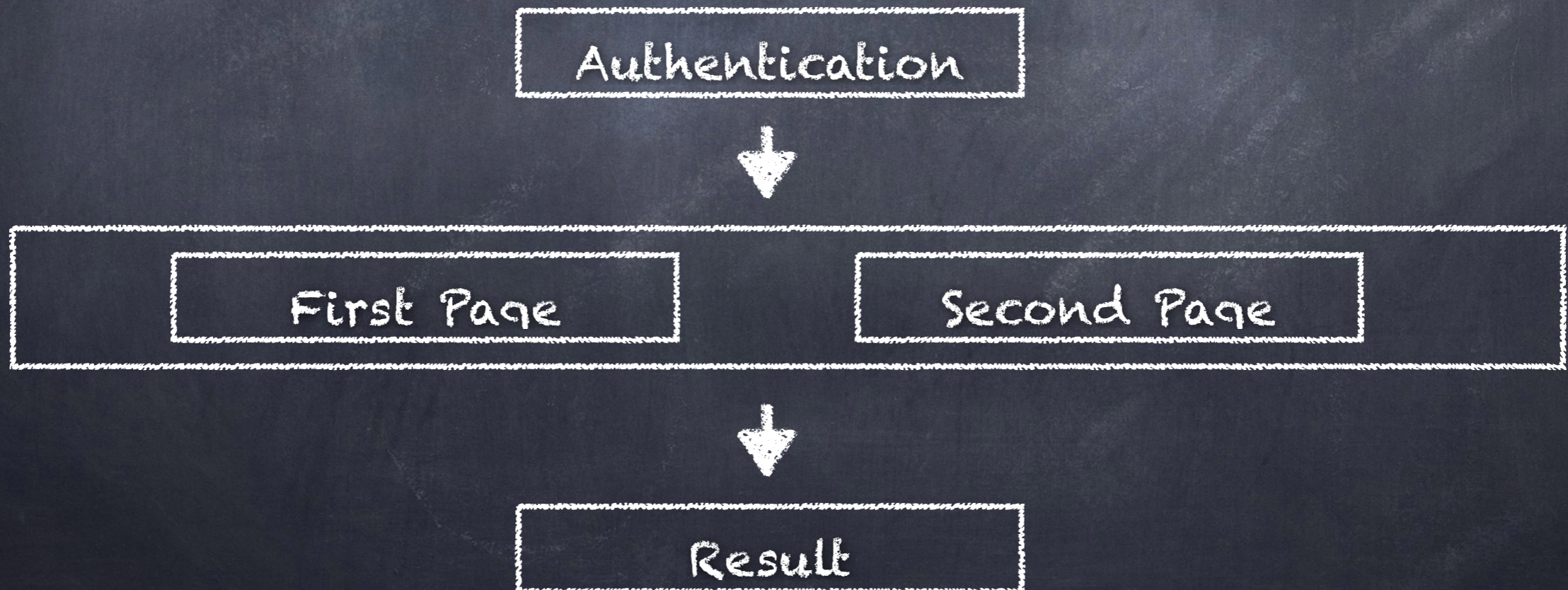
Result

Monads

Monads



Monads



FP Intuition

Dependency

flatMap

Monads

Parallelism

zip/traverse

Applicatives

Conclusion

While FP is about composition,
Parallelism is about evaluation.

Through the composition of

Monads with Applicatives

it's possible to achieve: Simple, reliable
and **STYLISH**

Concurrency and Parallelism.

Thank you!!!!

Questions?